

➤ In this study we presented a theoretical investigation of the channeling interaction potential between proton and the radial deformed (12,0)@(8,0)@(4,0) triple-wall carbon nanotubes (TWNTs). Multi-wall nanotubes (MWNTs) can be technically realised with better channeling performance than the single-wall nanotubes (SWNTs) and that is why we believe that these investigations can be useful for guiding of nanosized ion beams [1]. Obtained results show that the channeling potential is strongly influenced of level of radial deformation of nanotube [2, 3, 4].

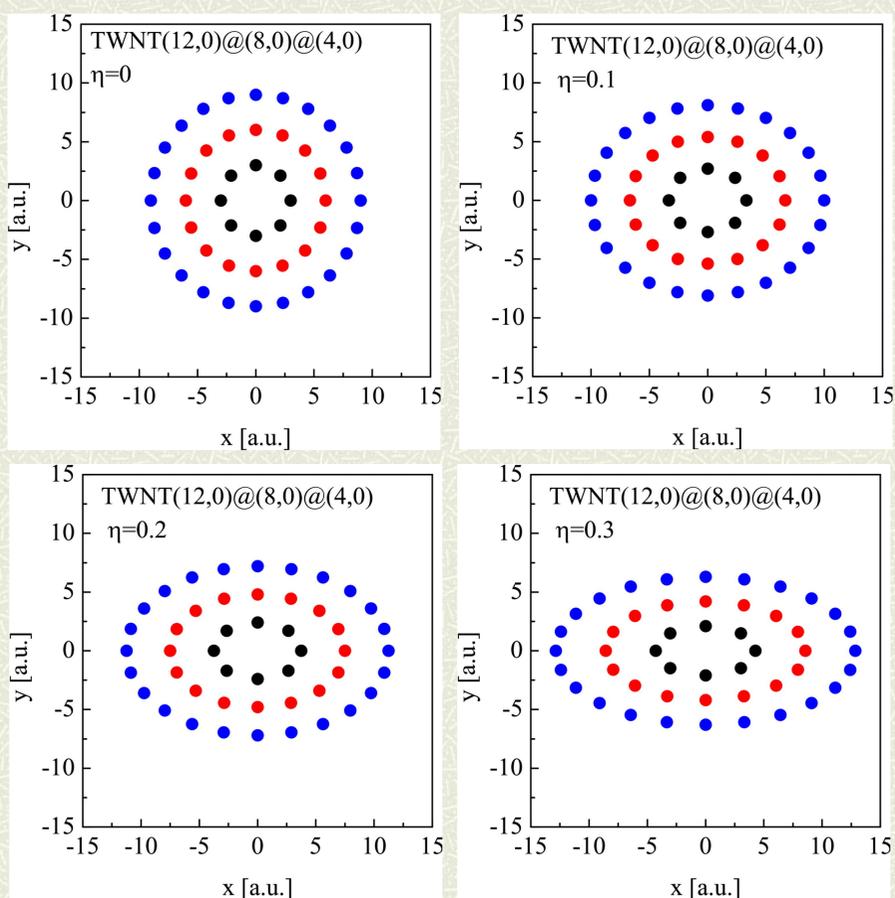


Figure 1. The view along axes of short TWNTs(12,0)@(8,0)@(4,0) under different radial strains: (left top) $\eta = 0$ (perfect nanotube); (right top) $\eta = 0.1$; (left down) $\eta = 0.2$; (right down) $\eta = 0.3$, respectively.

➤ We take that the interaction potential of the proton and a nanotube atom is of the Thomas-Fermi type and adopt for it the Molière's expression [5, 6, 7]:

$$V(r') = \frac{Z_1 Z_2 e^2}{r'} \left(0.35 e^{-0.3r'/a} + 0.55 e^{-1.2r'/a} + 0.10 e^{-6.0r'/a} \right)$$

$Z_1 = 1$ and $Z_2 = 6$ are the atomic numbers of the proton and nanotubes atoms, respectively

r – the distance between the proton and the nanotube atoms, $b = 0.3/a$ – parameter

$a = [9\pi^2/(128 Z_2)]^{1/3} a_0$ – the screening radius of the atom

a_0 – the Bohr radius (52.918 pm).

When we apply continuum approximation [6, 8] as a result, we obtain the proton- nanotube continuum interaction potential:

$$U(x, y) = \sum_{j=1}^J U_j(x, y); \quad U_j(x, y) = \frac{1}{d} \int_{-\infty}^{+\infty} V(\rho_j^2 + z^2)^{1/2} dz$$

$$\rho_j = \left((x - x_j)^2 + (y - y_j)^2 \right)^{1/2}$$

➤ The total number of atomic strings in the nanotube is indicated by J and in our case it is 48 (see Figure 1).

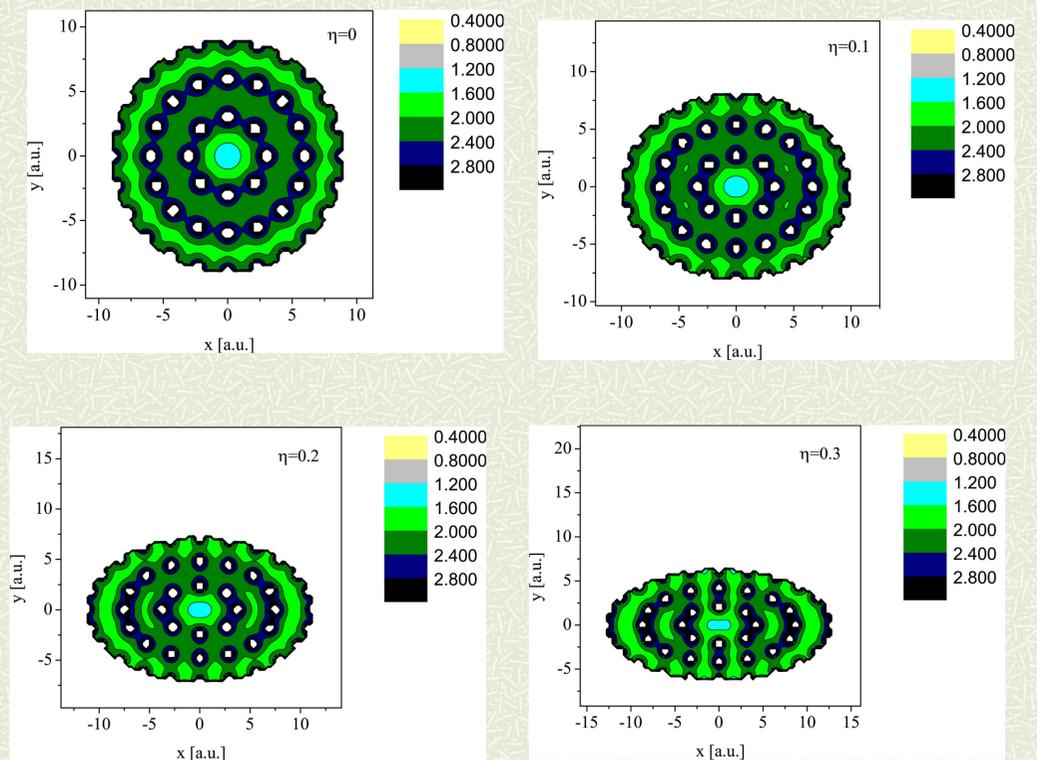


Figure 2. Contour plot of the channeling interaction potential $U(x, y)$ in the xy plane between proton and TWNTs(12,0)@(8,0)@(4,0) under different radial strains: (left top) $\eta = 0$; (right top) $\eta = 0.1$; (left down) $\eta = 0.2$; (right down) $\eta = 0.3$, respectively. Values for potential $U(x, y)$ within nanotube are presented in atomic units.

Radial deformation is characterized by the dimensionless parameter $\eta = (R - R_y)/R$ [9, 10, 11], where R_y is semi-minor axis and R is the radius of undeformed nanotube. Also, we can express the semi-axis as a function of the radius R and the parameter η : $R_x = R(1 - \eta) - 1$ and $R_y = R(1 - \eta)$.

The position of the carbon atom of the k -th atomic string in a plane perpendicular to the nanotube axis is determined by the angle θ_k and the distance from the nanotube center is R_k .

The interaction potential $U(x, y)$ can be calculated using following equation:

$$U(x, y) = \frac{4Z_1 Z_2 e^2}{d} \times \sum_{k=1}^N \sum_{j=1}^3 a_j K_0 \left(b_j \sqrt{x^2 + y^2 + R_k^2} - 2\sqrt{x^2 + y^2} R_k \cos \theta_k \right)$$

We can conclude that the nanotube channeling potential depends strongly on the radial strain.

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